

Forest Reflectance and Transmittance

FRT User Guide

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A. Kuusk and T. Nilson

Tartu Observatory

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Abstract

A directional multispectral forest reflectance model has been developed in the group of vegetation remote sensing at Tartu Observatory, Estonia. The early version of the forest reflectance model by Nilson (1991) has been extensively modified. The modified leaf optics models PROSPECT by Jacquemoud et al. (1996) and LIBERTY by Dawson et al. (1998), atmosphere radiative transfer model 6S by Vermote et al. (1994, 1997), and homogeneous two-layer canopy reflectance model ACRM by Kuusk (2001) have been incorporated into the model. The new model works in the spectral region 400-2400 nm with the same set of input parameters, the spectral resolution is 1 nm. Any Sun and view directions are allowed. The following manual presents the modification FRT23 of the model, the 2025 version. While the main principles of the model are those of the 2013 version (FRT13), there are some changes in the computer code, and the format of input files is changed.

1 Introduction

The transfer of solar radiation within forest stands is a rather complex process. We need models to understand how the reflected signal is formed and which are its most important driving factors. In addition, to create a satellite or aerial imagery-based forest management system, forest reflectance models capable of acting as an interface between the images and forestry databases are required. These models should be able to make maximum use of the forestry data contained in the database and allow to simulate the optical images, e.g. in terms of standwise ground-level reflectance factors. Originally, the forest reflectance model described in Nilson and Peterson (1991) has been derived just from these starting points. Several results of the previous work by Nilson and Kuusk (1989) were used in the model. The previous version of the model needed several improvements. First of all, to make use of multiangular remote sensing data, the model should be modified into a multiangular version. Second, a multispectral version of the model is required to study the relations between leaf biochemical and high spectral resolution reflectance data. Several improvements were also needed to create a more user-friendly version of the model and to introduce some changes in the calculation algorithms. For these purposes, a considerable modification of the original model was undertaken.

2 General layout of the model

The forest reflectance model may be classified as a hybrid-type model, including the properties both geometrical and radiative transfer equation-based models. Tree crown envelopes are

modelled as ellipsoids of rotation or cones in the upper and cylinders in the lower part (Fig. 1). Leaves and branches are uniformly distributed in the crown.

Several tree classes of different size and/or species are possible (Fig. 1). Within each class, trees are considered identical.

A homogeneous layer of vegetation is present on the ground surface.

The radiances of the forested scene components – tree leaves/needles, branches and stems, ground vegetation, and soil – are estimated with the help of geometrical and radiative transfer concepts. Special attention is paid to the adequate modelling of single scattering reflectance components, whereas reflectance caused by multiple scattering of radiation in the canopy is more roughly modelled.

The directional spectral reflectance of a forest stand in the given direction r_2 is calculated as a sum of the single scattering reflectance $\rho_I(r_1, r_2)$ and diffuse reflectance $\rho_D(r_2)$,

$$\rho(r_1, r_2) = \frac{I_\lambda}{Q_\lambda} \rho_I(r_1, r_2) + \rho_D(r_2), \quad (1)$$

where $I_\lambda = I_\lambda(\theta_1) \cos(\theta_1)$ is direct down-welling flux, and $Q_\lambda = I_\lambda + D_\lambda$ is the total down-welling flux, D_λ is diffuse downwelling flux, r_1 and r_2 are unit vectors in the Sun and view direction, respectively, θ_1 is the Sun zenith angle.

The single scattering reflectance factor $\rho_I(r_1, r_2)$ accounts for the single scattering from tree layer foliage and stems $\rho_{CR}^1(r_1, r_2)$, and single scattering from ground vegetation $\rho_{GR}^1(r_1, r_2)$,

$$\rho_I(r_1, r_2) = \rho_{CR}^1(r_1, r_2) + \rho_{GR}^1(r_1, r_2). \quad (2)$$

Diffuse reflectance $\rho_D(r_1, r_2)$ accounts both for the multiple scattering of radiation and for the diffuse radiance of scattered/reflected sky radiation D_λ .

The model works in the optical domain of radiation, 400-2400 nm, spectral resolution is 1 nm.

3 Model components

3.1 Single scattering in tree crowns

The first-order reflectance component $\rho_{CR}^1(r_1, r_2)$ is calculated separately for all tree classes,

$$\begin{aligned} \rho_{CR}^1(r_1, r_2) &= \sum_{j=1}^m \rho_{CRj}^1, \\ \rho_{CRj}^1 &= \lambda_j \int \int \int_{V_j} u_j \Gamma_j(r_1, r_2) p_{00j}(x, y, z; r_1, r_2) dx dy dz / \cos \theta_1 \end{aligned} \quad (3)$$

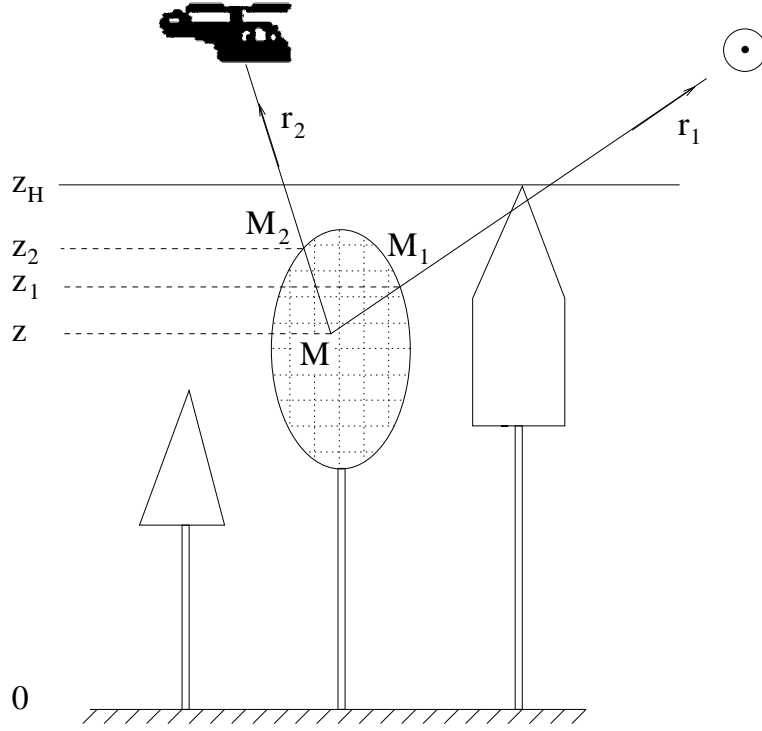


Figure 1: Deriving the first-order scattering component.

Here λ_j is the number of trees of the j th class per unit ground area, m is the number of tree classes, $u_j = u_j(x, y, z)$ is the foliage area volume density within a tree crown, $\Gamma_j(r_1, r_2)$ is the scattering (area) phase function of the canopy medium, $p_{00j}()$ is the bidirectional gap probability of two simultaneous free lines-of-sight in directions r_1 and r_2 from the point $M = (x, y, z)$ within a crown of the j th tree class (Fig. 1), V_j is the spatial region corresponding to the crown envelope. Integral (3) is calculated numerically using 3D quadrature.

The scattering phase function $\Gamma_j(r_1, r_2)$ in formula (3) is the sum of diffuse $\Gamma_{j,D}(r_1, r_2)$ and specular $\Gamma_{j,sp}(r_1, r_2)$ scattering,

$$\Gamma_j(r_1, r_2) = \Gamma_{j,D}(r_1, r_2) + \Gamma_{j,sp}(r_1, r_2). \quad (4)$$

The phase function of diffuse scattering is defined by Ross (1981) as

$$\begin{aligned} \Gamma_D(r_1, r_2) &= \frac{\rho_L}{2\pi} \int_{\Omega_R} g_L(r_L) |\cos(r_1 r_L) \cos(r_2 r_L)| d\Omega_L \\ &+ \frac{\tau_L}{2\pi} \int_{2\pi - \Omega_R} g_L(r_L) |\cos(r_1 r_L) \cos(r_2 r_L)| d\Omega_L, \end{aligned} \quad (5)$$

r_1 and r_2 are unit vectors in sun and view directions, $g_L(r_L)$ is the 2D distribution density of leaf normals, ρ_L and τ_L are the leaf reflectance and transmittance. The solid angle Ω_R is determined

by the condition $\cos(r_1 r_L) \cos(r_2 r_L) > 0$. In the assumption of uniform distribution of leaf normals the 2D distribution density of leaf normals $g_L(r_L)$ recedes to the 1D distribution $g_L(\theta_L)$, where θ_L is the leaf inclination (the polar angle of leaf normal).

The scattering phase function $\Gamma_D(r_1, r_2)$ in Eq. (5) may be calculated by analytical formulas in case of a few exceptional leaf angle distributions (LAD) (spherical, horizontal, vertical LAD, or fixed leaf angle) (Nilson, 1991).

Foliage orientation is described by the two-parameter elliptical distribution of leaf normals (Kuusk, 1995a),

$$g_L(\theta_L) = B_g / \sqrt{1 - \epsilon^2 \cos^2(\theta_L - \theta_m)}, \quad (6)$$

where θ_L is leaf inclination, θ_m is the modal leaf inclination, and ϵ is the eccentricity of the LAD which determines the shape of the LAD, B_g is a normalising factor. As the sensitivity range on the LAD eccentricity is very close to the limit value $\epsilon = 1$, the parameter $e_L = -\log(1 - \epsilon)$ is used as the input parameter of FRT.

The scattering phase function $\Gamma_{j,D}(r_1, r_2)$ in Eq. (5) is calculated by approximation formulae by Kuusk (1995a)

$$Y(\theta_m, \epsilon) = Y_0 + \beta_0 + (\beta_1 |m_L(\theta_m, \epsilon) - m_L(\epsilon = 0)| + \beta_2 |\sigma_L(\theta_m, \epsilon) - \sigma_L(\epsilon = 0)|)(Y_1 - Y_0). \quad (7)$$

Here, Y is the generic for the components of phase function in Eq. 5, Γ_R and Γ_T , respectively. Y_0 is the double integral in Eq. (5) in case of spherical orientation and Y_1 in case of fixed inclination (δ -distribution) at modal leaf angle. Coefficients β_j are tabulated in Table 1.

For conifer species the asymmetric Henyey-Greenstein phase function is used (Lenoble, 1977),

$$\Gamma_{HG}(\gamma) = \frac{1 - g^2}{\sqrt{(1 + g^2 - 2g \cos(\gamma))^3}}, \quad (8)$$

where g is the asymmetry parameter, $-1 \leq g \leq 1$, γ is the angle between sun and view directions.

Leaf reflection ρ_{Lj} and transmission τ_{Lj} coefficients are calculated with the PROSPECT submodel (Jacquemoud and Baret, 1990), or by the LIBERTY submodel (Dawson et al., 1998).

Optical parameters are averaged over all foliage elements (leaves, branches) according to their share in the total foliage area.

The phase function of specular reflection is

$$\Gamma_{sp}(r_1, r_2) = \frac{g_L(\theta_q)}{8} K(\alpha_0) \gamma_{sp}. \quad (9)$$

Here, γ_{sp} is the leaf reflection coefficient for the specular reflection determined by the refraction index of leaf surface wax $n_L(\lambda)$, α_0 is the incidence angle on the leaf, θ_q is the polar angle of the normal for the leaves specularly reflecting to the direction r_2 , and $K(\alpha_0)$ is the modification factor to account for the reduction of specular reflection by the acicular structure of the leaf. Leaf refractive index $n_L(\lambda)$ is a given tabulated function of wavelength.

The bidirectional gap probability $p_{00}(r_1, r_2)$ in Eq. (3) is defined as a product of two independent probabilities

$$p_{00}(r_1, r_2) = p_1(r_1, r_2) p_2(r_1, r_2) \quad (10)$$

$p_1(r_1, r_2)$ being the within-crown level bidirectional gap probability and $p_2(r_1, r_2)$ that of the between-crown level. In calculations of the bidirectional gap probability p_1 , results from (Kusk, 1991) for the crown of a single tree are applied. The mutual shading of needles in shoots and the characteristic linear dimension of foliage elements l_{sh} are accounted for.

$$p_1(r_1, r_2) = p_1(r_1) p_1(r_2) C_{HS}(\alpha), \quad (11)$$

where $p_1(r_1)$ and $p_1(r_2)$ are the gap probabilities in directions r_1 and r_2 inside the crown and $C_{HS}(\alpha)$ is the hot-spot correction, which account for the mutual correlation of gap probabilities in directions r_1 and r_2 , α is the angle between these two directions.

$$p_1(\theta) = \exp(-G_L(\theta) \kappa u_L l(\theta)), \quad (12)$$

u_L is the foliage area density (leaves/needles and branches), κ is the correction parameter which accounts for the mutual shading of needles or leaves in a shoot, $l(\theta)$ is the path length in the crown in direction r_i , $G_L(\theta)$ is the Ross-Nilson geometry function – the projection of the unit area of foliage in direction θ .

$$G_L(\theta) = \frac{1}{2\pi} \int_{2\pi} g_L(r_L) |\cos(r r_L)| d\Omega \quad (13)$$

G-function is calculated with approximation formula Eq. (7).

J_L is an integral function needed for the calculation of scattering coefficients in the calculation of diffuse fluxes, see Eq. (21).

The hot-spot correction $C_{HS}(\alpha)$ depends on the gap fractions in sun and view direction, the angle between these direction α and the mean leaf size l_L ,

$$C_{HS}(\alpha) = \exp \left\{ \sqrt{\frac{G_L(r_1) G_L(r_2)}{\mu_1 \mu_2}} \frac{u_L (1 - \exp(-\xi))}{\xi} \right\}, \quad (14)$$

Table 1: Values of coefficients of approximation Formula (7), Standard Error (SE), and Determination Coefficient r^2 .

Y	G_L	Γ_R	Γ_T	J_L
β_0	0.00072	-0.0102	0.00011	-0.0151
β_1	0.0463	0.0304	0.0047	0.0225
β_2	0.0250	-0.00795	0.1016	0.0317
SE	0.037	0.025	0.0046	0.0017

$\xi = \Delta/s_L$, $\Delta = \sqrt{1/\mu_1^2 + 1/\mu_2^2 - 2\cos(\alpha/(\mu_1\mu_2))}$, s_L is the leaf size parameter, μ_i are the direction cosines.

The between-crown gap probability, p_2 , in Eq. (10) stands for the parts of the lines-of-sight that lie outside the crown of interest, i.e. from the point $M_1(x_1, y_1, z_1)$ until the upper boundary of the forest canopy in the solar direction and from $M_2(x_2, y_2, z_2)$ in the view direction (Fig. 1). In this version of the model the calculation of the between-crown gap probability p_2 is modified. Instead of calculation the p_2 separately for every tree class a mean tree class is built, and the gap probability p_2 is calculated in assumption that all trees in the stand have the crown of mean size and mean foliage density. The trees of mean tree class have ellipsoidal crowns, the radius of which is equal to the mean radius of tree crowns. The length of the mean crown is determined by the vertical distribution of foliage in the stand. In order to avoid artefacts caused by exceptional tree classes, the wings of the foliage vertical distribution are cut. Total area of leaves and branches is distributed uniformly in the mean crown. The level of cutting is set in the source code of the module strmean.f, the parameter plevel.

Based on (Nilson, 1977) the between-crown gap probability p_2 is calculated as follows:

$$p_2 = a_s(z_1, \theta_1) a_s(z_2, \theta_2) C_{HS2}(z_1, z_2, l_{12}, r_1, r_2), \quad (15)$$

where $a_s(z, \theta)$ is the average proportion of gaps in the forest canopy at the height z in the direction θ , and C_{HS2} is the hot-spot correction factor for between-crown shading,

$$C_{HS2}(z_1, z_2, l_{12}, r_1, r_2) = \exp(\lambda c_m S_{cm}(z_1, z_2, l_{12}, r_1, r_2) p_{0m}), \quad (16)$$

λ is the total number of trees, $S_{cm}(z_1, z_2, l_{12}, r_1, r_2)$ is the area of the common part of the crown envelope projections in solar and view directions, corresponding to the heights z_1 and z_2 and the horizontal distance l_{12} ; p_{0m} is the joint probability of gap occurrence within the mean tree crown when viewed simultaneously from a point at the height z_1 in the solar direction r_1 and from another point at the height z_2 in the view direction r_2 , horizontal distance of the points being l_{12} . The parameter c_m is introduced to account for the deviations in the tree distribution pattern from the Poisson distribution, see Eq. (26).

The gap probability $a_s(z, \theta)$ is calculated on the assumption of the binomial distribution of trees (Nilson, 1977),

$$a_s(z, \theta_r) = \exp(-\lambda[b_{1j}(z, \theta_r)S_{crown,m}(z, \theta_r) + S_{trunk,m}(z, \theta_r)]) , \quad (17)$$

where λ is the total number of trees, $b_{1m}(z, \theta_r) = \ln[1 - (1 - a_{1m}(z, \theta_r))(1 - c_m)]/(1 - c_m)$, $S_{crown,m}(z, \theta_r)$ is the area of crown envelope projection for mean tree class at the level z , and $S_{trunk,m}(z, \theta_r)$ is the area of trunk projection of the mean class at the level z , $a_{1m}(z, \theta_r)$ is the gap probability in crowns in the direction θ_r at the level z , θ_r is the polar angle of the view vector $r_i, i = 1, 2$. The area of trunk projection $S_{trunk,m}(z, \theta_r)$ is calculated using trunk tapering curves by Ozolins (1988). The function $a_{1m}(z, \theta_r)$ is shown in Eq. (18),

$$a_{1m}(z, \theta_r) = \langle \exp(-u_m G(\theta_r)l(z, \theta)) \rangle . \quad (18)$$

Angle brackets mark averaging over the crown projection area $S_{crown,m}(z, \theta_r)$, $l(z, \theta)$ is the path length in the mean crown at level z , $G(\theta_r)$ is the Ross-Nilson geometry function. In case of spherical LAD $G(\theta_r) = 1/2$, for other LAD-s the approximation Eq. (7) is used. As the crown envelopes are supposed to be surfaces of revolution, the between-crown gap probability $a_s(z, \theta_r)$ does not depend on the azimuth. Grouping and/or regularity of the stand is described by a grouping parameter c_m , $c_m < 1$, $c_m = 1$, and $c_m > 1$ correspond to a regular, random, and clumped pattern of trees, respectively. As the stem coverage (basal area) is very small, unlike the crowns, the stem position pattern is supposed to be random.

In Eq. (17), the expression $\lambda[S_{crown,m}(z, \theta_r) + S_{trunk,m}(z, \theta_r)]$ stands for the mean coverage of ground by the shadows cast by crown envelopes and trunks of mean trees, if the direction of sunrays coincide with the view direction θ_r . It is the effective coverage that should appear in the exponent of Eq. (17). The mean coverage should be diminished, because the tree crowns are supposed to be semi-transparent, and modified to account for the tree distribution pattern effect. The two effects of single-crown transparency and of the tree distribution pattern on the between-crown canopy gap fraction are introduced by the parameter $b_{1m}(z, \theta_r)$. Note that $b_{1m}(z, \theta_r) = 1 - a_{1m}(z, \theta_r)$, if $c_m = 1$.

The overlapping of crown projections in Sun and view directions $S_{cm}()$ in Eq. (16) (Fig. 2), which is needed for the calculation of between-crown level bidirectional gap probabilities, can be calculated in case of ellipsoidal crowns and the approximation of crown projections by circles as in FRT13 is not needed.

The overlapping area $S_{cm}()$ in Eq. (16) is rapidly decreasing function of the angle between directions r_1 and r_2 , it is approximated by a simple trigonometric function

$$S_{cm}(.) \propto \left(\frac{\cos(\alpha)}{1 + \alpha} \right)^4 \quad (19)$$

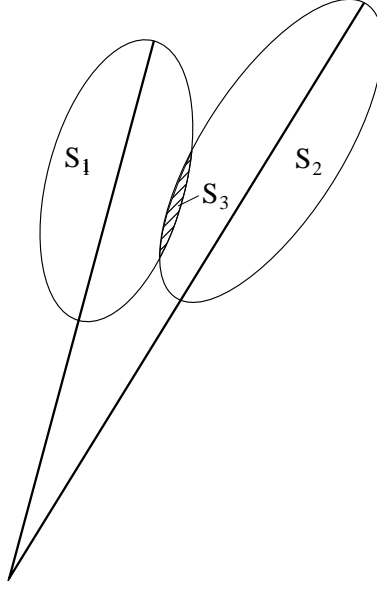


Figure 2: Calculation of the overlapping of crown projections.

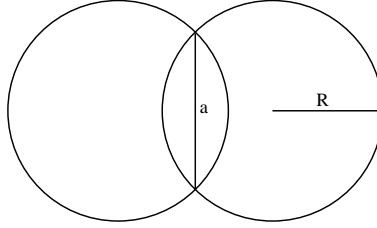


Figure 3: Common part of crown volumes.

Another modification is in the calculation of the gap probability in the mean crown $a_{1,m}(z, \theta_r)$, Eq. (18). Instead of using the mean path length in the crown, the transparency in the direction θ , $\exp(-u_m G(\theta_r)l(z, \theta))$ is averaged over the tree crown projection.

Equation (3) is valid in sparse stands of separate tree crowns. In dense stands the tree crowns are partly overlapping. To avoid the double accounting of overlapping parts of tree crowns, the probability $p_{00}()$ in Eq. (3) is corrected. The measure of overlapping is the ratio of canopy closure $CaCl$ to crown closure $CrCl$.

The chord length of the common part of crone volumes a in Fig. 3 is calculated with an approximate formula

$$a = c_1 \left(1 - \frac{CaCl}{CrCl} \right)^{c_2}. \quad (20)$$

Other components of the version FRT23 are equivalent to the version FRT13.

3.2 Single scattering on ground vegetation

The two-layer homogeneous canopy reflectance model ACRM by Kuusk (2001) is applied for the calculation of the bidirectional reflectance of ground vegetation. Input parameters of the ACRM are the leaf area index (LAI), leaf size, two leaf angle distribution parameters, the set of biophysical parameters (PROSPECT parameters) for two layers of ground vegetation, and weights of Price's functions for the calculation of the soil reflectance spectrum. The probability of seeing sunlit ground vegetation is calculated as the p_2 in Eq. (15) for the ground surface, $z_1 = z_2 = l_{12} = 0$. The direct to total incident radiation considers the downward scattering in the tree layer, Eqs. (30)-(31).

3.3 Diffuse fluxes

Diffuse fluxes of multiple scattering and of diffuse sky radiation are considered in four flux approximation like in the SAIL model (Verhoef, 1984) and in the ACRM model (Kuusk, 2001). Four differential equations define four fluxes: vertical fluxes up E_+ and down E_- , a direct solar flux E_s , and a flux associated with the radiance in the direction of observation E_o ,

$$\begin{aligned} dE_+/dz &= -au_LE_+ + \sigma u_LE_- + s'u_LE_s \\ dE_-/dz &= -\sigma u_LE_+ + au_LE_- - su_LE_s \\ dE_s/dz &= ku_LE_s \\ dE_o/dz &= vu_LE_- + uu_LE_+ - Ku_LE_o \end{aligned} \quad (21)$$

The SAIL coefficients a , σ , s' , s , k , v , u , and K are expressed using the G-function and leaf reflection and transmission coefficients ρ_L and τ_L . Equations (21) can be solved analytically, the general solutions for E_+ , E_- and E_s are given, e.g. in (Bunnik, 1978).

The diffuse component of reflectance ρ_d is a sum of two components, related to tree layer and to ground vegetation, ρ_d^{trees} and ρ_d^{gr} , respectively,

$$\rho_d = \rho_d^{\text{trees}} + \rho_d^{\text{gr}}, \quad (22)$$

where

$$\begin{aligned} \rho_d^{\text{trees}} &= \text{SQ} r_{so} + (1 - \text{SQ}) r_{do} + \\ &+ [\text{SQ} (p_1 r_{sd}^{\text{gr}} + t_{sd} r_{dd}^{\text{gr}}) + (1 - \text{SQ}) t_{dd} r_{dd}^{\text{gr}}] t_{do} / (1 - r_{dd} r_{dd}^{\text{gr}}) \end{aligned} \quad (23)$$

Table 2: Scattering operators of the tree layer

Definition	Boundary conditions
$r_{dd} = E_+(0)/E_-(0)$	$E_s(0) = 0, \quad E_+(-1) = 0, \quad E_-(0) = D_\lambda$
$t_{dd} = E_-(-1)/E_-(0)$	$E_s(0) = 0, \quad E_+(-1) = 0, \quad E_-(0) = D_\lambda$
$r_{sd} = E_+(0)/E_s(0)$	$E_s(0) = I_\lambda, \quad E_+(-1) = 0, \quad E_-(0) = 0$
$t_{sd} = E_-(-1)/E_s(0)$	$E_s(0) = I_\lambda, \quad E_+(-1) = 0, \quad E_-(0) = 0$
$r_{do} = E_o(0)/E_-(0)$	$E_s(0) = 0, \quad E_+(-1) = 0, \quad E_-(0) = D_\lambda$
$t_{do} = E_o^-(0)/E_-(0)$	$E_s(0) = 0, \quad E_+(-1) = 0, \quad E_-(0) = D_\lambda, \quad E_o^-(0) = 0$
$r_{so} = E_o(0)/E_s(0)$	$E_s(0) = I_\lambda, \quad E_+(-1) = 0, \quad E_-(0) = 0, \quad E_o(-1) = 0$

and

$$\rho_d^{\text{gr}} = [\text{SQ}(p_1 r_{sd}^{\text{gr}} r_{dd} + t_{sd}) + (1 - \text{SQ}) t_{dd}] r_{ds}^{\text{gr}} p_2 / (1 - r_{dd} r_{dd}^{\text{gr}}). \quad (24)$$

Here $\text{SQ} = I_\lambda/Q_\lambda$, $p_i = p(r_i)$ is the gap probability in direction r_i , r_{sd}^{gr} , r_{ds}^{gr} and r_{dd}^{gr} are the directional-hemispherical, hemispherical-directional, and hemispherical-hemispherical reflectance of ground vegetation, respectively. The ground vegetation reflectances r_{sd}^{gr} , r_{ds}^{gr} , and r_{dd}^{gr} are calculated by integrating the ACRM model over hemisphere by view, incident, and both directions, respectively.

The scattering operators of the tree layer r_{so} , r_{do} , t_{do} , t_{sd} , and t_{dd} are defined in Table 2 where $D_\lambda = Q_\lambda - I_\lambda$.

When calculating diffuse fluxes, the plant material is supposed to be distributed homogeneously in the horizontal, no layers, no trees, no branches, no shoots, and driving parameters are determined as averages approximating the behaviour of the canopy in bulk. The effective foliage area index value LAI_{eff} is used in the calculations of diffuse fluxes. LAI_{eff} is calculated from the gap probability in a given direction, it depends on the G-function of foliage and on the tree distribution pattern (clumping/regularity). As the G-function is almost invariant relative to leaf orientation at zenith angle 40° (Ross and Nilson, 1968), the effective LAI is calculated from the gap fraction at $\theta_0 = 40^\circ$,

$$LAI_{eff} = \frac{\sum_j (\kappa_{cl,j} LAI_j + BAI_j)}{\Omega_E}, \quad (25)$$

where

$$\begin{aligned} \Omega_E &= \frac{\sum_j (\kappa_{cl,j} LAI_j + BAI_j)}{\cos \theta_0 \sum_j \lambda_j S_{crown,j}(\theta_0) c_j(\theta_0)}, \\ c_j(\theta_0) &= \frac{-\ln(1 - (1 - a_{1j}(\theta_0))(1 - GI_j))}{1 - GI_j}. \end{aligned} \quad (26)$$

Here $\kappa_{cl,j}$ is the clumping coefficient of leaves/needles in a shoot of the tree class j , BAI_j is the branch area index, θ_1 is the Sun zenith angle, and $a_{1j}(\theta_1)$ is the gap probability in the Sun direction in crowns of the tree class j , GI_j is the Fisher's grouping index - the relative variance of the number of trees in the area $S_{crown,j}(\theta)$. The effective value of the foliage area index $LA_{eff}^{(mult)}$ is calculated from the assumption that the gap fraction in the direction of sunrays as calculated by means of Eq. (17), and the modified exponential formula, as proposed in Chen and Cihlar (1996), should be equal. Thus, Ω_E could be interpreted as the 'clumping index caused by structures larger than a shoot'.

3.4 Leaf optics

Leaf optics models PROSPECT (Jacquemoud and Baret, 1990) or LIBERTY (Dawson et al., 1998) can be used for the calculation of leaf reflectance and transmittance in tree crowns. There is no option of using the LIBERTY model for the ground vegetation. Both these models are modified so that the number of leaf constituents and names of files of their extinction spectra are listed in the input file. Extinction spectra of the models PROSPECT2 (Jacquemoud et al., 1996), PROSPECT3 (Fourty and Baret, 1998), and LIBERTY (Dawson et al., 1998) are available. The structure parameter of a single leaf in the PROSPECT model N is corrected to an effective value N_{eff} in order to account for the overlapping of leaves/needles in a shoot,

$$N_{eff} = N / \kappa_{cl} . \quad (27)$$

If compared with the PROSPECT model, the LIBERTY model has two additional parameters: average internal cell diameter and intercellular air space determinant (Dawson et al., 1998).

In the forest model input, the biochemical parameters are expressed as a fraction of the dry matter of leaves/needles. Using the described set of biophysical parameters, the whole spectrum of leaf reflectance and transmittance in the spectral range 400-2400 nm is calculated with the spectral resolution of 1 nm.

No good optical model for branch and trunk bark reflectance is available so far. Therefore, reflectance spectra of branch and trunk reflectance for every tree class are tabulated in separate input files.

3.5 Sky radiation

The wavelength-dependent relative share of direct and diffuse flux in incoming radiation is needed, Eq. (1). The atmospheric radiative transfer model 6S by Vermote et al. (1997) is involved for the calculation of incident radiation fluxes. Input parameters of the 6S model,

which are needed for the calculation of down-welling fluxes, are the percentage of four main aerosol components (dust-like, oceanic, water-soluble, and soot), and horizontal visibility or aerosol optical thickness at 550 nm τ_{aer}^{550} . The calculation of hemispherical-directional forest reflectance for sky radiation ρ_D is simplified. Instead of double integration over the hemisphere for incident directions, integration is performed in the perpendicular plane ($\varphi = 90^\circ$) only,

$$\rho_D(r_2) = \frac{\int_{2\pi} d(r_1) \rho_I(r_1, r_2) \mu_1 dr_1}{D_\lambda} \approx \frac{\int_0^{\pi/2} d(\theta_1, \varphi = \pi/2) \rho_I(\theta_1, \theta_2, \varphi = \pi/2) \mu_1 d\theta_1}{D_\lambda}, \quad (28)$$

where $d(r_1)$ is the sky radiance in the direction $r_1 = (\theta_1, \varphi_1)$, $\mu_1 = \cos \theta_1$, and $D_\lambda = \int_{2\pi} d(r_1) \mu_1 dr_1$ is the diffuse down-welling flux from the sky.

4 Transmittance of a forest canopy

The same algorithms can be used for the calculation of downward radiances and fluxes under a forest canopy. The relative downward radiance in direction r_2 Sun being in direction r_1 is presented as the sum of three components:

$$t(r_1, r_2) = t_{CR}^1(r_1, r_2) + t_{sky}(r_1, r_2) + t_{CR}^M(r_1, r_2). \quad (29)$$

Here the downward radiance $t(r_1, r_2)$ is normalised as reflectance in Eqs (2, 1), $t_{CR}^1(r_1, r_2)$ is the radiance of single scattering from tree crowns, $t_{sky}(r_1, r_2)$ is the sky radiance, and $t_{CR}^M(r_1, r_2)$ is the radiance of multiple scattering on crowns. In the model the sky radiance $t_{sky}()$ depends only on the Sun zenith angle θ_1 .

Total transmittance of the tree layer $t_Q(r_1, r_2)$ is calculated as a ratio of the downward flux below the tree canopy to the incoming total flux Q_λ ,

$$t_Q(r_1) = \frac{I}{Q_\lambda} \left(t_{CR}^I(r_1) + a_s(0, \theta_1) \right) + \frac{D_\lambda}{Q_\lambda} \int_{2\pi} \left(a_s(0, r_2) + t_{CR}^I(r_2) \right) \cos(\theta_2) dr_2, \quad (30)$$

and diffuse transmittance of the tree layer $t_D(r_1)$ is calculated as a ratio of the downward flux below the canopy (direct sunrays blocked) to the incoming diffuse flux D_λ ,

$$t_D(r_1) = \int_{2\pi} \left(a_s(0, r_2) \cos(\theta_2) + t_{CR}^I(r_2) \right) \cos(\theta_2) dr_2 + \frac{I_\lambda}{D_\lambda} t_{CR}^I(r_1). \quad (31)$$

Here $t_{CR}^I(r)$ is the scattering operator $I_\lambda(r) \rightarrow$ (downward scattered flux) for tree crowns.

5 Inversion of the model

Inversion of the model can be performed similar to Goel and Strebel (1983) or Kuusk (1991): a merit function is built, which has its minimum value when the best fit of measured and calculated reflectance data is reached. This way the complicated task of the solution of an array of non-linear equations for the estimation of model parameters is reduced to a more simple problem of the search of an extremum of a multidimensional function. In the merit function constraints are used in order to avoid the non-physical values of input parameters, and uncertainties of reflectance data and an expert estimate of parameter values are accounted for,

$$F(X) = \sum_{j=1}^m \left(\frac{\rho_j^* - \rho_j}{\epsilon_j} \right)^2 + \sum_{i=1}^n \left[(x_i - x_{i,b})^4 w_i^2 + \left(\frac{x_i - x_{e,i}}{dx_i} \right)^2 \right]. \quad (32)$$

Here $X = (x_1, x_2, \dots, x_n)$ is the vector of model input parameters, m is the number of the measured reflectance values ρ_j^* , ρ_j is the model reflectance value, ϵ_j is the error of the measured reflectance value ρ_j^* , x_i is a model parameter and $x_{i,b}$ its value on the boundary of the given region; w_i is a weight, $w_i = 0$ in the given region $x_i \in [x_{i,min}, x_{i,max}]$ and $w_i = \text{const}$ else, $x_{e,i}$ is the expert estimate of the parameter x_i , and dx_i is a tolerance for the parameter x_i which controls the sensitivity of the merit function on the expert estimate.

There is an option to use only absolute differences $(\rho_j^* - \rho_j)^2$ in the merit function.

In the inversion, the redundancy of data can be effectively used, i.e. the number of reflectance values inverted may be more than the number of model parameters subject to estimation. Anyway, as the number of model parameters is large, most of the model parameters should be fixed at ‘best guess’ values, and only a few parameters can be estimated simultaneously. Only the parameters of the first tree class can be estimated in the inversion.

6 Conclusion

The model can be used for the interpretation of multispectral and/or multiangular remote sensing data in the wide range of Sun and view angles in the whole optical domain 400-2400 nm. The proposed version of the model seems to be a good tool for different sensitivity analyses, e.g. an analysis of the dependence of BRDF, in particular near the hot spot, on the stand structural variables at different structural levels and on optical parameters of the canopy and understory can be made.

The same computer code can be used both for direct and inversion modelling.

The model is coded in Fortran. The computational aspects of the model are detailed in the following appendices:

- General description of the computer code
- Example of inputs and outputs
- Complete description of the subroutines

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Appendix

A General description of the computer code

A rough flowchart of the computer code is in Fig. 1, the call-tree of the main program in Fig. 2, and the call-tree of the module frtsv – the single direct run of the model called in the module func(), in Fig. 3.

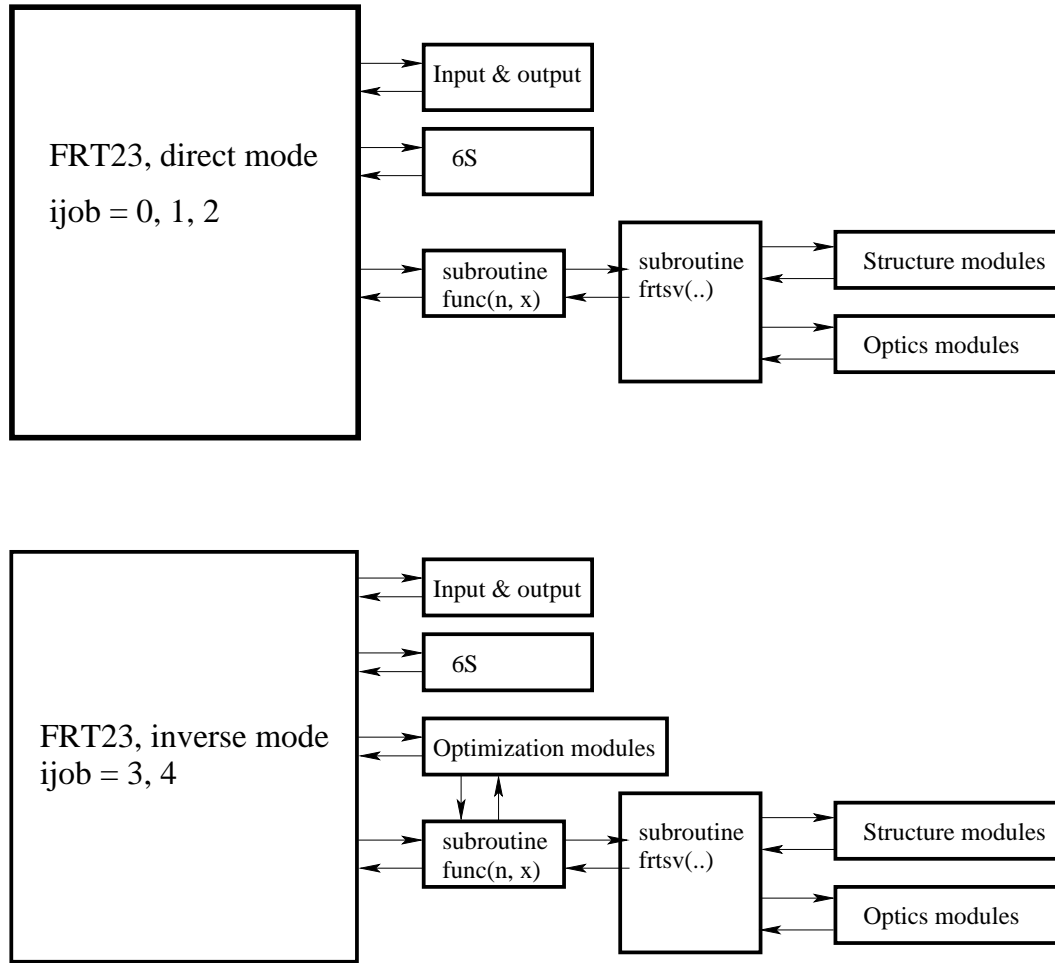


Figure 1: Flowchart of the computer code.

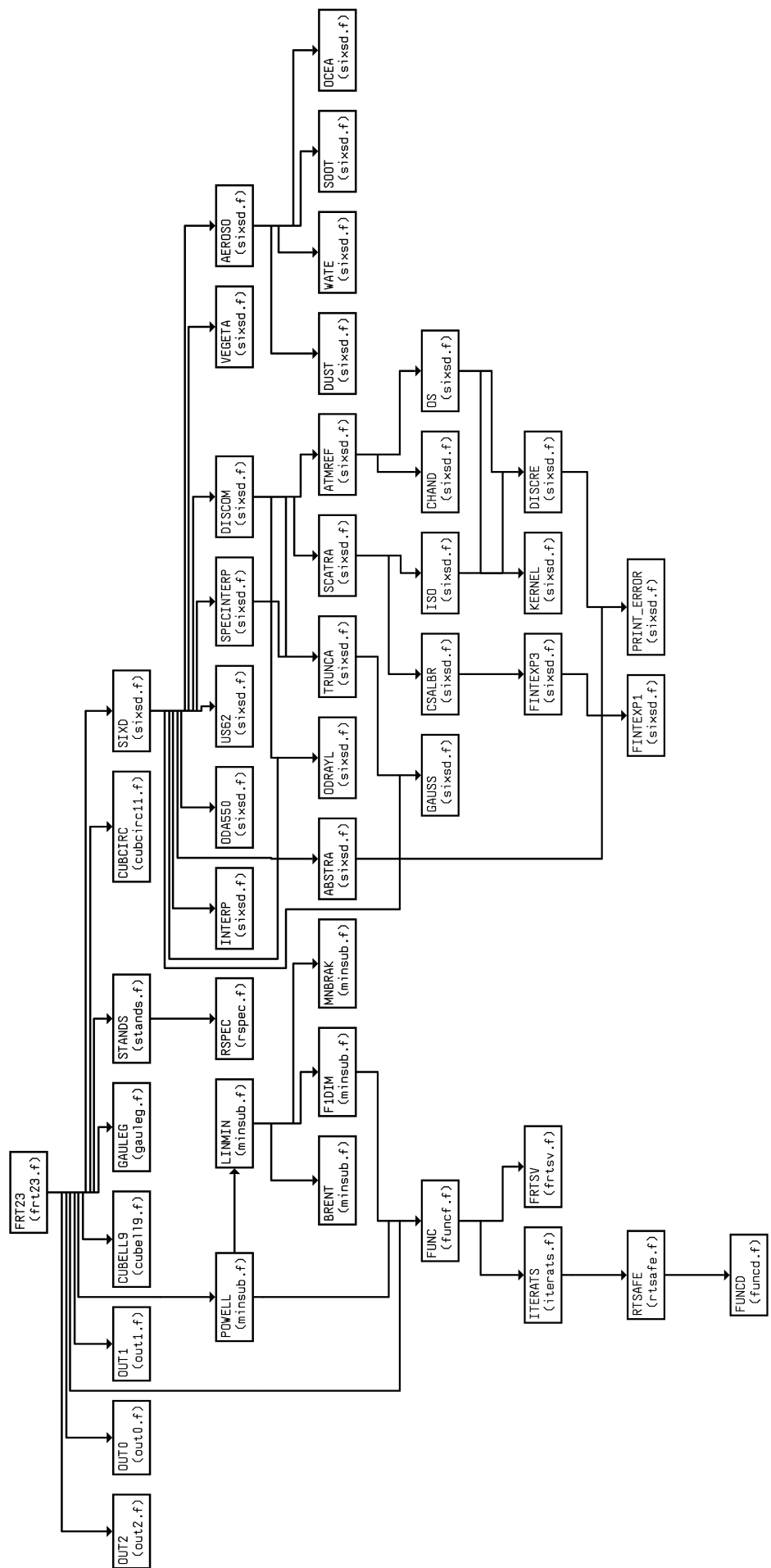


Figure 2: The call-tree of the computer code.

B The usage

The model is distributed as a compressed tar-archive of source texts, sample input and output files. It is recommended to create a separate directory for the model. Move the archive `frt23?????.tar.gz` to this directory, extract the files and make

```
tar -xzf frt23?????.tar.gz
make frt23 or make all
```

`make clean` removes object files,
`make distclean` removes object files and executables.

If you don't use the gfortran compiler then you should modify the makefile.

To run the code type on the commandline

```
./frt23 inputfile outputfile
```

If you do not give input and output files on commandline then you will be asked for the file-names.

Program `frt23` calculates in direct mode forest reflectance and transmittance. There are options to perform calculations in various modes:

- a single run for given Sun and view angles and fixed wavelength
- reflectance spectrum for given view and Sun angles in the given range of wavelengths or for a list of spectral bands
- angular distribution of reflectance at given azimuth (relative to the Sun azimuth) for a given Sun zenith angle in the range of view polar angles 0 .. 80°

Any view and Sun angle is allowed, however, do not use polar angles very close to 90°.

There are several input files required: a file of stand parameters (the stand file), the files of tree parameters for the second, third *etc* tree classes, files of absorption spectra for the leaf optics model, the files of refraction index spectrum and of Price' vectors, and files of bark and trunk reflectance spectra.

The same code is used for the inversion: parameters of the first tree class and/or ground vegetation can be estimated.

B.1 The stand file

The same stand file can be used both for the direct and inverse modes. Some input parameters are needed only in the inverse mode. These parameters are ignored in the direct mode and thus can be missing in the direct mode. The files of the second and other tree classes have the same structure as the stand file for the direct mode, the redundant data may be missing, in case they are present they are not used.

The input parameter *ijob* controls which task will be run:

<i>ijob</i>	task
0	a single run, Sun and view angles, and wavelength fixed to the first value of the respective parameter in the input file
1	calculate spectrum, Sun and view angles fixed
2	calculate angular distribution for $\theta = -80 \dots 80^\circ$, Sun zenith, azimuth and wavelength fixed
3	inversion of the model using BRF values in the fixed view direction, the initial guess, the recommended range of parameters, and errors of the reflectance values are accounted for in the merit function; BRF values at different wavelengths are used
4	inversion of the model, absolute differences in the merit function

***ijob* = 1**

The spectral range is determined by the wavelength of the first spectral band, the wavelength increment dwl , and the number of spectral bands. The valid range of wavelengths is 400 - 2400 nm, spectral resolution 1 nm. The spectrum step is given by an input parameter dwl , if $dwl \leq 0$ then the list of wavelengths should be given.

***ijob* = 2**

Program calculates the angular distribution of forest reflectance and transmittance in the range $-80 \dots 80^\circ$ at a given azimuth (relative to the principal plane) and given increment in the view nadir angle. Negative polar angles correspond to the backscattering (hot-spot side), and positive polar angles - to the forward scattering.

***ijob* = 3**

The code is run in inverse mode, n parameters of the first tree class which are listed in the key vector $ll(n)$ are estimated by minimizing the merit function $F(X)$, Eq. (32).

***ijob* = 4**

As $ijob = 3$, except absolute differences are accounted for in the merit function $F(X)$, i.e. $\epsilon = 1$ in Eq. (32).

Structure of the stand file

A sample stand file is printed in the page 24. Colons are used to mark comments, information after a colon is not used by the computer code. Below the sample stand file is commented linewise. The row of the input file is printed in bold. As the number of lines is not constant - it depends on the number of leaf components - the lines in comments are not numbered. The numbers in the right column are the position of the respective parameter in the vector of model parameters.

The first group of parameters describe the task and situation. The second group is the description of the first tree class. The third group is the description of the ground vegetation. In case of inversion the fourth group provides inversion parameters, and the fifth group the input reflectance data.

In the files of other tree classes the lines of the first group are scrolled forward, tree parameters are in the same format as in the file of the first tree class, the other groups of parameters may be missing.

A sample stand file

```

'RAMI KS'                                : data set name
49                                         : stand age
7                                           : # of size classes
*** files of refractive index and other tree classes ***
'refrind.dat' 'algl1' 'potr1' 'tico2' 'bepe2' 'algl2' 'piab3'
0                                           : *ijob*: 0-single, 1-spectrum, 2-ad, 3,4-inversion (3-relat., 4-abs. differences)
4                                           : .80 .17 .0 .03 : iaer, c(i) - aerosol data (6S)
0.                                         : .06 : v, tau_aer(550) - visibility (6S)
37.6                                       : Sun zenith
0.                                         : 2. 7. : view nadir angle, its increment, and view azimuth angle
6                                           : -1. : # of spectral bands and spectrum step
486. 571. 650. 838. 1677. 2217.           : spectral bands (TM)
x0 xmin xmax dx i
'KS'                                       : species
t_elli                                    : crown form
.0399 .0001 .08 .02 : stand density,  $m^{-2}$  1
26.5 10. 30. 5. : tree height, m 2
9.0 .5 10. 9. : crown l, m; ell l con 3
0. .5 10. 1. : cylinder 4
1.7 .2 5. .3 : crown radius, m 5
20.7 2. 25. 5. : trunk diameter, cm 6
3.014 1.1 5. 8. : m - total dry leaf weight, kg/tree 7
76. 30. 120. 60. : SLW - leaf weight per area, g m-2 8
0. .0 4.5 .5 : eln3 - -ln(1 - eps) 9
53.57 0. 90. 20. : thm3 - modal leaf angle 10
.2 .05 .6 .2 : shoot length, m 11
0.15 .01 1. .05 : BAI/LAI 12
1.3 .6 2.8 .05 : tree distr. param.  $GI_j$  13
.0 .0 .6 .05 : H-G asymmetry (phase function) 14
.95 .6 1. .2 : shoot shading coef 15
.9 .6 1.2 .2 : refr. index ratio 16
1.658 1.2 2.8 .5 : leaf str. param. - PROSPECT N 17
40. 20.0 60. 5. : d_cell Liberty 18
0.03 .01 0.06 .02 : a_cell Liberty 19
'birchbr1.dat' : file of branch reflectance
'birchtr1.dat' : file of trunk reflectance
'prospect' : leaf optics model
3 : # of leaf components
144.0 50. 320. 50. 'waterb.dat' : c1, % of SLW, component 1 20
0.60 .3 1. .2 'chlorp3.dat' : c2, % of SLW, component 2 21
54.65 34. 99.8 20. 'drymatter.dat' : c3, % of SLW, component 3 22
*** Ground vegetation ***
1.61 .01 6. .3 : LAI2_ground, upper layer 30
.15 .02 .4 .05 : sl2 - HS-parameter 31
1.0 .4 1. .2 : clmp2 - foliage clumping parameter 32
0.60 0. 2. .3 : szz - vertical regularity 33
3.99 .0 4.5 .5 : eln2 - -ln(1 - eps) 34
57.34 0. 90. 20. : thm2 - modal leaf angle 35
.90 .6 1.3 .2 : n_ratio2 36
76.0 60. 120. 30. : SLW2( $g/m^2$ ) 37
1.315 1. 2.8 .2 : N2 (PROSPECT) 38
'prospect' : leaf optics model, upper layer
4 : # of leaf components
5.0 3. 30. 10. 'waterb.dat' : c1, % of SLW, component 1 39
.633 .3 .8 .2 'chlorp3.dat' : c2, % of SLW, component 2 40
17.60 0. 40. 2. 'anthocyanin.dat' : c3, % of SLW, component 3 41
81.80 74. 99.8 20. 'drymatter.dat' : c4, % of SLW, component 4 42
0.53 .01 1.1 .3 : LAI1_ground, lower layer 49
.15 .02 .4 .05 : sl1 - HS-parameter 50
0.6 .4 1. .2 : clmp1 - foliage clumping parameter 51
3.0 .0 4.5 .5 : eln1 - -ln(1 - eps) 52
90. 0. 90. 20. : thm1 - modal leaf angle 53

```

0.9	.6	1.3	.2	: n_ratio1	54
65.29	60.	120.	30.	: SLW1(g/m^2)	55
1.0053	1.	2.5	.2	: N1 (PROSPECT)	56
'prospect'				: leaf optics model, lower layer	
5				: # of leaf components	
85.23	60.	120.	50.	'waterb.dat' : c1, % of SLW, component 1	57
.40	.3	.8	.2	'chlorp3.dat' : c2, % of SLW, component 2	58
0.44	.3	.8	.2	'anthocyanins.dat' : c3, % of SLW, component 3	59
98.72	94.	99.8	20.	'drymatter.dat' : c4, % of SLW, component 4	60
.44	.0002	4.	.1	'cellp3.dat' : c5, % of SLW, component 5	61
'soil.dat'		45.		: file of Price' vectors, th*	
1.13	0.95	1.4	.1	: s1 - soil parameters	67
.0	-.1	.1	.02	: s2	68
.0	-.05	.05	.02	: s3	69
.0	-.04	.04	.02	: s4	70

* !!! the following linesi are not required for direct problem !!! ***

'powell'				: name of the optimization subroutine
5000	1	100	100	: nfm, itmax, itbr, nbra
1.E-9	1.E-7	1.E-13	1.E-8	: zeps, tolbr, tiny, ftolp
1.	.5	2.	.2	: alpha, beta, gamma, dx
2	20.			: n, at
1	7			: ll(i)
486.	.0271	.02		: th_Sun=38.
572.	.2744	.1		: th_Sun=38.
661.	.2806	.1		: th_Sun=38.
838.	.0228	.02		: th_Sun=38.
1677.	.2702	.1		: th_Sun=38.
2217.	.2765	.1		: th_Sun=38.

lambda reflectance delta_rho

'RAMI KS' : data set name
49 : stand age
7 : # of size classes

The number of tree classes, the max number of tree classes is 10.

*** files of refractive index and other tree classes *** – a comment line

'refrind.dat' 'algl1' 'potr1' 'tico2' 'bepe2' 'algl2' 'piab3'

This line cannot be omitted in the case of one tree class.

1 : *ijob*: 0-single, 1-spectrum, 2-ad,
3,4-inversion (3-relat., 4-abs. differences)

The job control parameter *ijob*:

- 0 - calculate a single value of canopy reflectance
- 1 - calculate reflectance spectrum for the given Sun and view angles
- 2 - calculate reflectance angular distribution at given azimuth
- 3 - inversion of the FRT model, relative differences in the merit function
- 4 - inversion of the FRT model, absolute differences in the merit function

The next group of parameters are the input parameters of the 6S model (Vermote et al., 1997).

4 **.80 .17 0. .03** : iaer, c(i) - aerosol data (6S)

$iaer, c(i)$ – aerosol model (6S)

-1 BRDF, no sky radiation

0 no aerosols

1 continental model

2 maritime model

3 urban model

4 enter the volumic percentage of each component $c(i)$

$c(1)$ – fraction of dust-like

$c(2)$ – water-soluble

$c(3)$ – oceanic

$c(4)$ – soot

0. **.06** : visibility v , km, and/or $\tau_{aerosol}(550 \text{ nm})$ if $v \leq 0$
37.6 : Sun zenith

0. **2.** **7.** : view nadir angle, its increment, and azimuth angle.
The azimuth angle is counted from the principal plane, the allowed range is $[0..180]$.
6 **-1.** : # of spectral bands, spectrum step

Number of spectral bands; the spectrum step $d\lambda$. If $d\lambda < 0$ then give the list of spectral bands on the next line. Otherway, the spectrum has the fixed increment and only the first wavelength is read.

486. **571.** **650.** ... : spectral bands
x0 **xmin** **xmax** **dx** **i** - a comment
'KS' : tree species, a character string for information purposes only
t_elli : crown form,
A logical parameter of crown shape: t – ellipsoid, f – cylinder+cone

Starting from the next row there are four parameter values in each line. Only the first value ($x0$) is required for the direct run, x_{min} and x_{max} are the boundary values of the parameter in the inversion run. The fourth column, dx , is the tolerance of the parameter in the inversion, Eq. (32). The first value ($x0$) serves as an initial guess and as an expert estimate $x_{e,j}$, Eq. (32) of the parameter value in the inversion. There is the parameter number in the vector of parameters in the last column. Only the first column ($x0$) is needed in the direct mode ($ijob = 0, 1, 2$)

.0399 **.0001** **.08** **.08** : stand density, m^{-2}
Number of trees for the given tree class
26.5 **10.** **25.** **5.** : tree height, m
9.0 **.5** **10.** **9.** : crown l, m; ell | con
Crown length (ellipsoid) or length of the conical part of the crown (cylinder+cone)
0. **0.** **10.** **1.** : cylinder
Length of the cylindrical part of crown
1.7 **.2** **5.** **.3** : crown radius, m

Crown radius - the horizontal semiaxis of ellipsoid or the base radius of the cone

20.7	2.	25.	5.	: trunk diameter, cm
------	----	-----	----	----------------------

DBH – trunk diameter at the breast height.

3.014	1.1	3.	8.	: m - total dry leaf weight, kg/tree
76.	30.	120.	60.	: SLW - leaf weight per area, g m ⁻²
0.	.0	4.5	.5	: eln3 - -ln(1 - eps)

the eccentricity parameter of LAD

53.57	0.	90.	20.	: thm3 - modal leaf angle
.2	.05	.6	.2	: shoot length, m
.15	.01	1.	.05	: BAI/LAI ratio
1.48	.6	2.8	.05	: tree distr. param. GI_j

Grouping index, $GI_j = 1$ – a random stand, $GI_j < 1$ – a clumped stand, $GI_j > 1$ – a regular stand.

.0	.1	.6	.05	: H-G asymmetry (phase function)
----	----	----	-----	----------------------------------

If this parameter is ≤ 0 , then the Ross-Nilson area scattering phase function of plate medium is used.

.95	.6	1.	.2	: shoot shading coef
-----	----	----	----	----------------------

Shoot shading parameter κ , accounts for the decrease of effective G-function due the mutual shading of leaves (needles) , $\kappa = 1$ – no mutual shading.

1.	.6	1.2	.2	: refr. ind. ratio
----	----	-----	----	--------------------

Refraction index of the leaf surface wax is calculated from the tabulated value by multiplying to this coefficient.

1.6016	1.6	2.8	.5	: leaf str. param. - - PROSPECT N
40.	20.	60.	5.	: d_cell Liberty
0.03	0.01	0.06	.02	: a_cell Liberty
'birchbr1.dat'				: file of branch reflectance
'birchtr1.dat'				: file of trunk reflectance
'prospect'				: leaf optics model, options are 'prospect' and 'liberty'.
3				: # of leaf components n_{comp}

In the next n_{comp} lines the percent concentration of the component and the file name of the component absorption spectrum for every component is listed. Despite in the direct mode only the first parameter $x(0)$ is used, the filename must be at the fifth position in the line. The components 20-29 of the vector of parameters are reserved for the leaf biochemical constituents - the tree layer, components 39-48 - the upper layer of ground vegetation, and components 57-66 - the lower layer of ground vegetation, so the maximum number of leaf biochemical components is 10. The components 18 and 19 of the vector of parameters are the LIBERTY parameters cell diameter and amount of inter-cell air, for the tree layer. In ground vegetation only the Prospect model is accepted.

144.	50.	320.	50.	'waterb.dat'	: c1, % of SLW, model component 1
0.60	.3	1.	.2	'chlorp3.dat'	: c2, % of SLW, model component 2
54.65	40.	99.9	20.	'drymatter.dat'	: c3, % of SLW, model component 3

The next group of parameters are the input parameters of the two-layer CR model (Kuusk, 2001).

**** Ground vegetation ***			- a comment
1.61	.01	6.	6. : LAI2_ground, upper layer
.15	.02	.4	.4 : sl2 - HS-parameter
1.0	.4	1.	.2 : clmp2 - foliage clumping parameter
1.2	0.	2.	.3 : szz - vertical regularity
3.99	.0	4.5	.5 : eln2 - $-\ln(1 - \text{eps})$
53.34	0.	90.	20. : thm2 - modal leaf angle
.9	.6	1.3	.2 : n_ratio2
76.0	60.	120.	30. : $\text{SLW2}(g/m^2)$
1.315	1.	2.8	.2 : N2 (PROSPECT)
'prospect'			: leaf optics model, upper layer
4			: # of leaf components
5.	1.	120.	50. 'waterb.dat' : c1, % of SLW, component 1
.633	.3	.8	.2 'chlorp3.dat' : c2, % of SLW, component 2
17.60	0.	40.	20. 'anthocyanins.dat' : c3, % of SLW, component 3
81.80	60.	99.8	20. 'drymatter.dat' : c4, % of SLW, component 4
0.53	.01	1.	.3 : LAI1_ground, lower layer
.15	.02	.4	.05 : sl1 - HS-parameter
0.6	.4	1.	.2 : clmp1 - foliage clumping parameter
3.0	.0	4.5	.5 : eln1 - $-\ln(1 - \text{eps})$
90.	0.	90.	20. : thm1 - modal leaf angle
.9	.6	1.3	.2 : n_ratio1
65.29	60.	120.	30. : $\text{SLW1}(g/m^2)$
1.0053	1.	2.5	.2 : N1 (PROSPECT)
'prospect'			: leaf optics model, lower layer
5			: # of leaf components
85.23	60.	120.	50. 'waterb.dat' : c1, % of SLW, component 1
.4	.3	.8	.2 'chlorp3.dat' : c2, % of SLW, component 2
0.44	.3	.8	.2 'anthocyanins.dat' : c3, % of SLW, component 3
98.72	94.	99.8	20. 'drymatter.dat' : c4, % of SLW, component 4
.44	.0002	4.	.1 'cellp3.dat' : c5, % of SLW, component 5
'soil.dat'	45.		: file of Price' vectors, th*
1.1309	.05	.4	.07 : s1 - soil parameters
.0	-.1	.1	.02 : s2
.0	-.05	.05	.02 : s3
.0	-.04	.04	.02 : s4

The next group of parameters are optimization parameters. The only working option for the optimization subroutine is 'powell'.

'powell'			: name of the optimization subroutine
5000	1	100	100 : nfmax, itmax, itbr, nbrak
<i>nfmax</i> – the max number of calculations of merit function			
<i>itmax</i> – the max number of iterations			
<i>itbr</i> – the max number of iterations in the subroutine brent			
<i>nbrak</i> – number of iterations in the subroutine mnbracket			
1.E-9	1.E-7	1.E-13	1.E-8 : zeps, tolbr, tiny, ftolp
1.	.5	2.	.2 : alpha, beta, gamma, dx

'prospect'				: leaf optics model	
3				: # of leaf components	
144.0	50.	320.	50.	'waterb.dat' : c1, % of SLW, component 1	20
0.60	.3	1.	.2	'chlorp3.dat' : c2, % of SLW, component 2	21
54.65	34.	99.8	20.	'drymatter.dat' : c3, % of SLW, component 3	22

B.3 Bark and trunk reflectance spectra

The files of bark and trunk reflectance spectra are simple two-column files of 2001 rows, where the first column is wavelength, nm, and the second column is reflectance. The wavelength interval is 1 nm.

C A sample output file

```
#
# Forest Reflectance Model FRT23 V.04.2025 by A. Kuusk, T. Nilson
#
# Input parameters:
# RAMI KS                      Stand Age = 49
## ijob = 2
# Sun zenith = 36.0 View azimuth = 0.0 View zenith step = 2.0
# Wavelength = 671.9 nm
# 7 tree class(es)
# Files of parameters of other tree classes:
#
#          alg11      potrl      tico2      bepe2      alg12
#          1          2          3          4          5          6
#          KS          LM          HB          PN          KS          LM
#          ellips      ellips      ellips      ellips      ellips      ellips
# 1 stand density, m-2 0.0399 0.0176 0.0079 0.0264 0.0066 0.0020
# 2 tree height, m    26.500 23.400 26.760 20.200 17.900 17.500
# 3 ell. or cone      9.000 15.000 8.220 13.000 5.600 8.500
# 4 cylinder, m       0.000 0.000 0.000 0.000 0.000 0.000
# 5 crown radius, m   1.700 2.107 2.100 2.130 1.100 1.500
# 6 trunk d, cm       20.700 22.400 21.600 14.500 10.500 13.100
# 7 total leaf weight 3.014 2.995 5.768 1.640 0.659 0.770
# 8 leaf weight, g m-2 76.000 77.400 76.200 25.500 76.000 77.400
# 9 eln              0.000 3.600 5.500 5.700 0.000 3.600
# 10 thm             53.570 6.800 8.190 6.300 53.570 6.800
# 11 shoot size, m    0.200 0.150 0.200 0.100 0.200 0.150
# 12 BAI/LAI          0.150 0.220 0.100 0.080 0.150 0.220
# 13 tree distr. param. 1.200 1.480 1.480 1.200 1.480 1.480
# 14 g_H-G            0.000 0.000 0.000 0.000 0.000 0.000
# 15 shoot shading coef 0.950 0.950 0.950 0.950 0.950 0.950
# 16 refr. ind. ratio 0.900 0.900 0.900 0.900 0.900 0.900
# 17 leaf str.par     1.658 1.762 1.548 1.543 1.658 1.762
# 18 D_cell, mcm      40.000 40.000 40.000 40.000 40.000 40.000
# 19 i-cell air       0.030 0.030 0.030 0.030 0.030 0.030
# bark refl. files: birchbr1.dat aldertr1.dat oambr1.dat oambr1.dat
# trunk refl. files birchtr1.dat aldertr1.dat oamtr1.dat oamtr1.dat
# Leaf models:      prospect prospect prospect prospect prospect
# # of leaf comp-s: 3          4          4          3          3
# 20 waterb.dat waterb.dat waterb.dat waterb.dat waterb.dat
#    144.0000 147.8000 56.8100 103.2000 144.0000
# 21 chlorp3.dat chlorp3.dat chlorp3.dat chlorp3.dat chlorp3.datat
#    0.6000 0.8772 0.2778 0.2890 0.6000
# 22 drymatter.dat drymatter.dat drymatter.dat drymatter.dat
#    54.6500 71.2900 18.5700 102.9000 54.6500
# 23 base.dat base.dat
#    0.0000 167.5000 20.5300 0.0000 0.0000 0.0000
#
```

```

# *** Ground vegetation, upper layer,          lower layer
# 30 ground LAI2          1.610          0.530
# 31 leaf size           0.150          0.150
# 32 clmp                1.000          0.600
# 33 szz                 0.600
# 34 eln                 4.000          3.000
# 35 thm                57.340          90.000
# 36 n_ratio            0.900          0.900
# 37 SLW                76.000          65.290
# 38 leaf str.par       1.315          1.005
# Leaf model: prospect
# 39 # of leaf components:      4          5
# 39 waterb.dat          5.000          waterb.dat          85.230
# 40 chlorp3.dat         0.633          chlorp3.dat          0.400
# 41 anthocyanins.dat    17.600          anthocyanins.dat          0.440
# 42 drymatter.dat       81.800          drymatter.dat          98.720
# 43                    cellp3.dat          0.440
# File of Price' vectors: soil.dat
# Sun angle of the soil reflectance: 45.0
# 67 sl_soil            1.1309
# 68 s2                 0.0000
# 69 s3                 0.0000
# 70 s4                 0.0000
#
#
# *** Results:
#
#          1          2          3          4          5
#          KS          LM          HB          PN          KS
#          ellips      ellips      ellips      ellips      ellips
# stand density, m-2    0.040      0.018      0.008      0.026      0.007
# tree height, m       26.500     23.400     26.760     20.200     17.900
# ell. or cone         9.000     15.000      8.220     13.000      5.600
# cylinder, m          0.000      0.000      0.000      0.000      0.000
# crown radius, m      1.700      2.107      2.100      2.130      1.100
# trunk d, cm          20.700     22.400     21.600     14.500     10.500
# lf_wght/tr&tot_m-2    3.014      2.995      5.768      1.640      0.659
# SLW, g m-2           76.000     77.400     76.200     25.500     76.000
# eln                  0.000      3.600      5.500      5.700      0.000
# thm                  53.570     6.800      8.190      6.300     53.570
# shoot size, m         0.200      0.150      0.200      0.100      0.200
# BAI/LAI              0.150      0.220      0.100      0.080      0.150
# tree distr. param.    1.200      1.480      1.480      1.200      1.480
# g_H-G                0.000      0.000      0.000      0.000      0.000
# shoot shading coef    0.950      0.950      0.950      0.950      0.950
# refr. ind. ratio      0.900      0.900      0.900      0.900      0.900
# leaf str.par         1.658      1.762      1.548      1.543      1.658
# D_cell, mcm          40.000     40.000     40.000     40.000     40.000
# i-cell air           0.030      0.030      0.030      0.030      0.030
# bark refl. files:    birchbrl.dat  aldertr1.dat  oambr1.dat  oambr1.dat
# trunk refl. files    birchtr1.dat  aldertr1.dat  oamtr1.dat  oamtr1.dat
# Leaf models:         prospect      prospect      prospect      prospect
# # of leaf comp-s:     3          4          4          3
#          waterb.dat  waterb.dat  waterb.dat  waterb.dat
#          144.0000     147.8000     56.8100     103.2000
#          chlorp3.dat  chlorp3.dat  chlorp3.dat  chlorp3.dat
#          0.6000       0.8772       0.2778       0.2890
#          drymatter.dat  drymatter.dat  drymatter.dat  drymatter.dat
#          54.6500      71.2900      18.5700      102.9000
#          -            base.dat      base.dat      -
#          0.0000       167.5000     20.5300      0.0000
# rl_eff = 0.1179  tl_eff = 0.0831  rsl = 0.1160
# leaf area density    0.692      0.325      1.047      0.536      0.672
# Total LAI            4.667
# Total BAI            0.600

```



```

#   crown closure = 1.150                                canopy closure = 0.749
#
# Warning!: canopy closure (CC) > crown closure (CR)
#           class, CC, CR:   7  0.2095E-01  0.1764E-01
#
#
# *** Ground vegetation, upper layer,                lower layer
#   ground LAI2, LAI1                1.610            0.530
#   leaf size                        0.150            0.150
#   clmp                             1.000            0.600
#   szz                              0.600
#   eln                              4.000            3.000
#   thm                             57.340            90.000
#   n_ratio                          0.900            0.900
#   SLW                             76.000            65.290
#   leaf str.par                     1.315            1.005
#   Leaf model: prospect
#   # of leaf components:              4                5
#   waterb.dat                       5.000            waterb.dat            85.230
#   chlorp3.dat                      0.633            chlorp3.dat            0.400
#   anthocyanins.dat                 17.600            anthocyanins.dat            0.440
#   drymatter.dat                    81.800            drymatter.dat            98.720
#                                     cellp3.dat            0.440
#   s1_soil                          1.1309
#   s2                              0.0000
#   s3                              0.0000
#   s4                              0.0000
#
#   Sun zenith = 36.0   View azimuth = 0.0   View zenith step = 2.0
#   Wavelength = 671.9 nm   S'/Q = 0.9
#   CaCl: 0.7485           CrCl: 1.1503
#
# thv   refl   r_grnd   rcr1   rgr1   rdif   b_down   gfr
-80.0  0.03906  0.01955  0.03066  0.00000  0.01028  0.02861  0.00000
-78.0  0.03633  0.01906  0.02794  0.00000  0.01011  0.02850  0.00000
-76.0  0.03430  0.01874  0.02596  0.00000  0.00992  0.02844  0.00000
-74.0  0.03262  0.01856  0.02437  0.00000  0.00974  0.02839  0.00000
-72.0  0.03128  0.01847  0.02313  0.00000  0.00956  0.02837  0.00000
[.]
72.0  0.02643  0.01296  0.01797  0.00000  0.00956  0.02824  0.00000
74.0  0.02821  0.01357  0.01967  0.00000  0.00974  0.02833  0.00000
76.0  0.03041  0.01434  0.02182  0.00000  0.00992  0.02845  0.00000
78.0  0.03322  0.01531  0.02462  0.00000  0.01011  0.02860  0.00000
80.0  0.03699  0.01651  0.02845  0.00000  0.01028  0.02882  0.00000

```

D Description of the subroutines

D.1 Subroutines of general use

D.1.1 Subroutine *stands*

reads input data

D.1.2 Subroutine *out0*

prints parameter values to the output file

D.1.3 Subroutine *out1*

prints the results of the direct run to the output file

D.1.4 Subroutine *out2*

prints the results of inversion to the output file

D.1.5 Subroutine *frtsv*

frtsv(..) is the procedure which performs the single direct run of the model.

D.1.6 Function *func* (*funcf.f*)

In the direct mode the function *func* extracts the model parameters from the vector of parameters and provides to the subroutine *frtsv*(..) for a single direct run.

In the inverse mode the function *func* checks that the model parameters are in the allowed range, scales the parameters subject to the estimation, and computes the merit function.

D.1.7 Subroutines *iterats*, *rtsafe* and *funcd*

Compute the Fisher's grouping index GI_j , Eq. (10) from the given structure parameter $c_j(\theta_1)$. The Newton-Raphson method is used, Press et al. (1992), Algorithm 9.4.

D.1.8 Subroutines *cubell9*, *cubcirc* and *gauleg*

Provide quadrature (cubature) knots and weights to numerical integrations.

D.1.9 Subroutine *rspec*

Reads tabulated spectra – absorption spectra of leaf constituents, stem and branch bark reflectance, Price' vectors *etc.*

D.2 Structure modules

D.2.1 Subroutine *strmean*

Computes the mean values of structure parameters.

D.2.2 Subroutine *regre*

Regressions for tree parameters. The call of this subroutine is commented out. Such regressions can be used in case some tree parameters are not available.

D.2.3 Subroutine *gggl*

The Ross-Nilson G-function for elliptical LAD.

D.2.4 Subroutine *hetk8s*

Calculates gap probabilities in Sun and view directions.

D.2.5 Subroutine *gfzx*

Calculation of the gap fraction at level zzx in direction thx .

D.2.6 Subroutine *pcrown*

Crown transparency, ellipsoid, at level zzx .

D.2.7 Subroutine *rlips*

Distance from (xi, yj, zk) to crown perimeter, ellipsoid, in direction $thet$, phi .

D.2.8 Subroutine *rcone*

Distance from (xi, yj, zk) to crown perimeter, cylinder+cone, in direction $thet$, phi .

D.2.9 Subroutine *int3de*

Integrates the bidirectional probability p_{00j} , over the whole tree crown, Eq. (3), ellipsoid.

D.2.10 Subroutine *int3dc*

Integrates the bidirectional probability p_{00j} , over the whole tree crown, Eq. (3), cone and cylinder.

D.2.11 Subroutine *bgf2*

Bidirectional free lines of sight outside the tree crown.

D.2.12 Subroutine *hsc12*

Hot-spot correction inside the crown.

D.2.13 Subroutine *overlap*

Correction of the probability to see sunlit element in crown in order not to count twice the common part of overlapping crowns.

D.2.14 Subroutine *pstem*

Probability of sunlit stem.

D.2.15 Subroutine *stem*

The area of stem longitudinal section.

D.2.16 Subroutine *pelld*

The projection *szdx* and volume *vzdi* of the lower part of an ellipsoid.

D.3 Optics modules

D.3.1 Subroutine *optmean*

Computes the mean and effective values of optical parameters.

D.3.2 Subroutine *aground*

Computes the directional-hemispherical reflectance *rsdgrou* and albedo (hemispherical-hemispherical reflectance) *rddgrou* of ground vegetation.

The double integral over hemisphere which is needed for the hemispherical-hemispherical reflectance of ground vegetation is substituted by an integral over polar angle at the azimuth $\varphi = 90^\circ$. The integral is calculated with an Gaussian quadrature.

D.3.3 Subroutine *hetk8o*

Single scattering radiance of tree crowns, up and down.

D.3.4 Subroutine *diffor*

Computes diffuse fluxes of multiple scattering and of scattered diffuse sky radiation.

Diffuse fluxes are computed in two-stream approximation (Bunnik, 1978; Kuusk, 2001).

D.4 Reflectance of ground vegetation (rmsub.f)

Subroutines

smcrm
biz2
gamma
gleaf
gmfres
soil
dif2
layer
rhoc1
skylspec

constitute the two-layer homogeneous canopy reflectance model ACRM. The full description of algorithms is published by Kuusk (1994, 1995a,b, 2001).

D.5 PROSPECT - the leaf optics model

Subroutines

prospect
tav
s13aaf

constitute the leaf optics model by Jacquemoud and Baret (1990).

D.6 LIBERTY - the leaf optics model

Subroutines

liberty
fresnel

constitute the leaf optics model by Dawson et al. (1998).

D.7 Atmosphere radiative transfer model 6S (sixsd.f)

General description of the 6S model is published by Vermote et al. (1997). The detail description of 6S modules is in (Vermote et al., 1994). For the calculation of incoming fluxes are used the modules

sixd
abstra
aeroso
atmref
chand
csalbr
discom
discre
dust
gauss

interp
iso
kernel
oce
oda550
odrayl
os
print_error
scatra
soot
specinterp
trunca
us62
vegeta
wate

D.8 Optimization modules

The Powell's method (Press et al., 1992), Algorithm 10.5 is used for the minimization of the merit function Eq. (16). The corresponding subroutines are

powell
linmin
mnbrak
function brent

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